

Long Division Review



QUICK NOTE! In long division, most of the time, we'll end up with remainders.

In elementary school you probably notated remainders with the letter R—for example, $7 \div 2 = 3 \text{ R } 1$ —and I'll use remainders here.

In this book, however, you'll learn to express remainders as fractions and decimals.

Sample problem 1:

When you see a problem like $432 \div 9$ or, equivalently, $9 \overline{)432}$, here's how you go about solving it:

Remember, 9 is called the *divisor* (see p. 126 for a tip on how to remember the name). The divisor is the number that is *dividing into* the bigger number, which is called the *dividend*.

divisor $\nearrow 9 \overline{)432} \nwarrow$ dividend

Let's divide!

$$9 \overline{)432}$$

First, let's see if the divisor goes into the first digit. Nope, 9 doesn't divide into 4, because 4 is smaller than 9, so we can just move on and check the first two digits, together.

$$4 \div 9 = ?$$

$$9 \overline{)432}$$

How many times does 9 go into 43? Think about your times tables. And find the biggest one that doesn't get bigger than 43.

$$9 \times 4 = 36$$

$$9 \times 5 = 45 \text{ (too big)}$$

$$\begin{array}{r} 4 \\ 9 \overline{)432} \\ - 36 \\ \hline 7 \end{array}$$

So use $9 \times 4 = 36$. Be sure to put the 4 on top, directly over the last digit of the number you divided the divisor into (in this case, the 4 goes right over the 3 of the number 43). Then subtract 36 from the 43 underneath, and we get 7.

$$43 - 36 = 7$$

$$\begin{array}{r} 4 \\ 9 \overline{)432} \\ - 36 \\ \hline 72 \end{array}$$

Now look at the next digit in the dividend—in this case 2. Draw an arrow down from the 2 and have it join the 7.

$$\begin{array}{r} 4 \\ 9 \overline{) 432} \\ - 36 \downarrow \\ \hline 72 \end{array}$$

Now ask, "How many times does 9 go into **72**?" Our times tables tell us that 9 times 8 equals 72.

$$9 \times 8 = 72$$

$$\begin{array}{r} 48 \\ 9 \overline{) 432} \\ - 36 \downarrow \\ \hline 72 \\ - 72 \\ \hline 0 \end{array} \rightarrow \text{DONE!}$$

Write the **8** directly above, and now subtract 72 from 72.

$$72 - 72 = 0$$

There are no more numbers to draw arrows from, and, in fact, there is no remainder. We're done!

Answer:

$$432 \div 9 = 48$$

Sample problem 2:

Often there will be a remainder, so let's do a division problem that has one: $8371 \div 14$, which is equivalent to: $14 \overline{) 8371}$.

$$14 \overline{) \mathbf{8}371}$$

First, let's see if the divisor goes into the first digit. Nope, 14 doesn't divide into **8** because 8 is smaller than 14, so we can move on and check the first *two* digits, together.

$$8 \div 14 = ?$$

$$14 \overline{)8371}$$

How many times does 14 go into 83? Let's test some numbers to find out.

$$14 \times 5 = 70$$

$$14 \times 6 = 84$$

(too big)

$$\begin{array}{r} 5 \\ 14 \overline{)8371} \\ - 70 \\ \hline 13 \end{array}$$

So use $14 \times 5 = 70$. Be sure to put the 5 on top, directly over the last digit of the number you divided the divisor into (in this case, the 5 goes right over the 3 of the number 83). Then subtract 70 from the 83 underneath, and we get 13.

$$83 - 70 = 13$$

$$\begin{array}{r} 5 \\ 14 \overline{)8371} \\ - 70 \downarrow \\ \hline 137 \end{array}$$

Now look at the next digit in the dividend, in this case 7. Draw an arrow down from the 7 and have it join the 13.

$$\begin{array}{r} 5 \\ 14 \overline{)8371} \\ - 70 \downarrow \\ \hline 137 \end{array}$$

Now ask, "How many times does 14 go into 137?" Let's test some numbers to find out. We'll use $14 \times 9 = 126$.

$$14 \times 8 = 112$$

$$14 \times 9 = 126$$

$$14 \times 10 = 140$$

(too big, and it should be a single digit

anyway—if 14 times 10 had been smaller than 137, that would mean you had made a mistake earlier and should go back and check your work.

(it will always be a single digit: 0-9)

$$\begin{array}{r}
 59 \\
 14 \overline{) 8371} \\
 \underline{- 70} \downarrow \\
 137 \\
 \underline{- 126} \\
 11
 \end{array}$$

Write the 9 directly above, and now subtract 126 from 137 and get 11.

$$137 - 126 = 11$$

$$\begin{array}{r}
 59 \\
 14 \overline{) 8371} \\
 \underline{- 70} \downarrow \\
 137 \\
 \underline{- 126} \downarrow \\
 111
 \end{array}$$

Now look at the next digit in the dividend—in this case 1. Draw an arrow down from the 1 and have it join the 11.

$$\begin{array}{r}
 59 \\
 14 \overline{) 8371} \\
 \underline{- 70} \downarrow \\
 137 \\
 \underline{- 126} \downarrow \\
 111
 \end{array}$$

Now ask, "How many times does 14 go into 111?" Let's test some numbers to find out.

$$14 \times 7 = 98$$

$$14 \times 8 = 112 \text{ (too big)}$$

$$\begin{array}{r}
 597 \\
 14 \overline{) 8371} \\
 \underline{- 70} \downarrow \\
 137 \\
 \underline{- 126} \downarrow \\
 111 \\
 \underline{- 98} \\
 13
 \end{array}$$

So use $14 \times 7 = 98$. Be sure to put the 7 directly overhead. Then subtract 98 from the 111 underneath, and we get 13.

$$\begin{array}{r}
 597 \\
 14 \overline{) 837} \\
 \underline{- 70} \downarrow \\
 137 \\
 \underline{- 126} \downarrow \\
 111 \\
 \underline{- 98} \\
 13
 \end{array}$$

There are no more numbers to draw arrows from, so the number on the bottom must be our **remainder**. Write the answer, and then add "R 13" for the remainder. We're done!

$$\begin{array}{l}
 \text{Answer: } 837 \div 14 \\
 = 597 \text{ R}13
 \end{array}$$

Sample Problem 3:

Let's do one more example, to demonstrate how zeros can pop up in the middle of long division: $616 \div 3$.

$$\begin{array}{r}
 2 \\
 3 \overline{) 616}
 \end{array}$$

First try dividing the divisor, 3, into the first digit of the dividend, 6. How many times does 3 go into 6? We'll use $3 \times 2 = 6$. Make sure to put the 2 directly over the last digit (in this case, the only digit) of the number we're dividing into.

$$3 \times 2 = 6$$

$$\begin{array}{r}
 2 \\
 3 \overline{) 616} \\
 \underline{- 6} \\
 0
 \end{array}$$

Now subtract 6 from the 6 in the dividend and get 0. Don't panic, just keep going as if it were any other number.

$$6 - 6 = 0$$

$$\begin{array}{r}
 2 \\
 3 \overline{) 616} \\
 \underline{- 6} \downarrow \\
 01
 \end{array}$$

The next step, as always, is to draw an arrow from the **next digit** in the dividend, and bring it down.

$$\begin{array}{r} 20 \\ 3 \overline{) 616} \\ - 6 \downarrow \\ \hline 01 \\ - 0 \\ \hline 1 \end{array}$$

Since 1 is smaller than 3, we can't divide 3 into 1. So how many times does 3 "go into" 1? **None**. So we use $3 \times 0 = 0$ and put a **0** up top. It works exactly the same way as with nonzero numbers.

$$3 \times 0 = 0$$

$$3 \times 1 = 3$$

(too big)

$$\begin{array}{r} 20 \\ 3 \overline{) 616} \\ - 6 \downarrow \\ \hline 01 \\ - 0 \\ \hline 16 \end{array}$$

Now draw an arrow down from the next digit in the dividend, **6**, and have it join the 1 to get 16.

$$\begin{array}{r} 20 \\ 3 \overline{) 616} \\ - 6 \downarrow \\ \hline 01 \\ - 0 \\ \hline 16 \end{array}$$

Now ask, "How many times does 3 go into 16?" Test some numbers.

$$3 \times 5 = 15$$

$$3 \times 6 = 18$$

(too big)

$$\begin{array}{r} 205 \\ 3 \overline{) 616} \\ - 6 \downarrow \\ \hline 01 \\ - 0 \\ \hline 16 \\ - 15 \\ \hline 1 \end{array}$$

So we use $3 \times 5 = 15$, and subtract 15 from the 16, to get 1.

$$16 - 15 = 1$$

$$\begin{array}{r}
 205 \text{ R } 1 \\
 3 \overline{) 616} \\
 \underline{-6} \downarrow \\
 01 \downarrow \\
 \underline{-0} \downarrow \\
 16 \downarrow \\
 \underline{-15} \\
 1
 \end{array}$$

There are no more digits in the dividend to draw arrows from, so the number on the bottom must be the **remainder**. Write the answer and then "R 1" for the remainder. We're done!

$$\begin{aligned}
 &\text{Answer: } 616 \div 3 \\
 &= 205 \text{ R } 1
 \end{aligned}$$